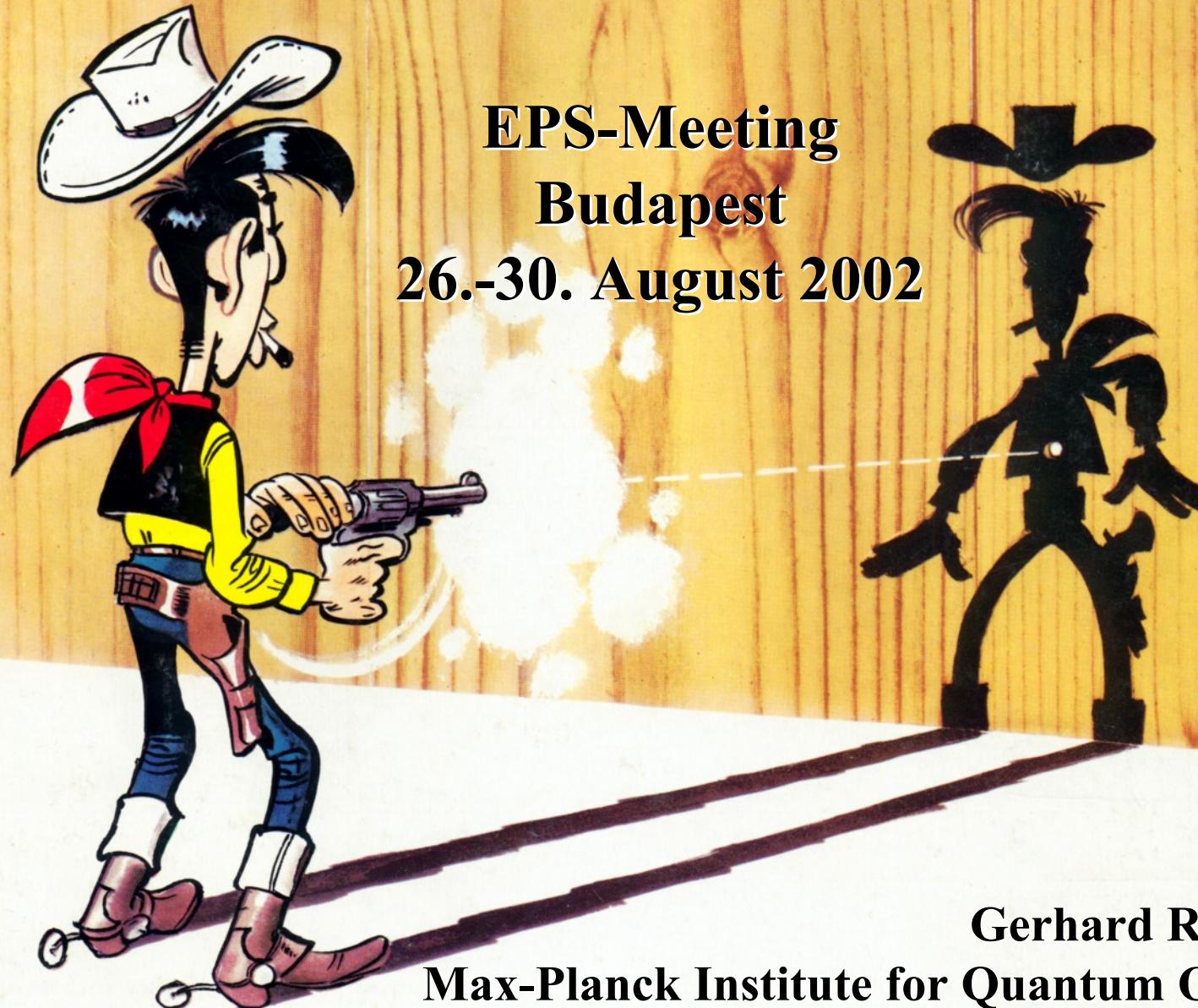


# Optical Cavity Quantum Electrodynamics



EPS-Meeting

Budapest

26.-30. August 2002

Gerhard Rempe  
Max-Planck Institute for Quantum Optics  
Garching, Germany

# Optical Cavity Quantum Electrodynamics

## why is it interesting ?

- network of **unitary** quantum computers
- control of a **dissipative** quantum system

## what has been achieved in the laboratory ?

- example 1: light-matter interface
- example 2: feedback control of atomic motion

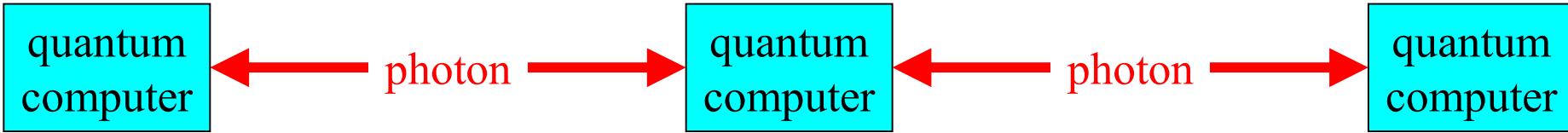
## where can it be applied in the future ?

- example 3: microscopy of a moving atom

# Distributed Quantum Network

## quantum computer

most likely, it will employ a **small** number of qubits



## quantum network

adds modularity and scalability

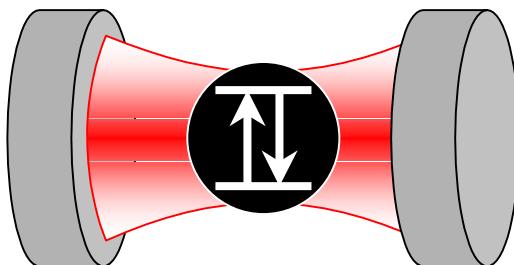
### wanted: light-matter interface

a photon source based on a unitary  
(deterministic and reversible)  
emission process

# Ingredient I: Cavity Quantum Electrodynamics

atomic - dipole decay rate :

$$\uparrow \quad \gamma = \frac{1}{4\pi\epsilon_0} \frac{2}{3} \frac{\mu^2 \omega^3}{\hbar c^3}$$



cavity - field decay rate :

$$\kappa = \frac{\omega}{2Q} = \frac{c}{2L} \frac{\pi}{F}$$

atom - photon coupling constant :

$$g = \frac{\mu E}{\hbar} = \mu \sqrt{\frac{\omega}{2\epsilon_0 \hbar V}}$$

↑

vacuum - electric field :

$$\frac{\hbar\omega}{2} = \int \epsilon_0 E^2 dV \Rightarrow E = \sqrt{\frac{\hbar\omega}{2\epsilon_0 V}}$$

**strong coupling  $g > (\gamma, \kappa)$ :**

**cavity-volume  
small**  
↓  
 **$g$  large**

**cavity-finesse  
high**  
↓  
 **$\kappa$  small**

**internal dynamics faster than  
coupling to the environment**

# Cavity QED for Quantum Information Processing

## microwave domain (ENS, LMU):

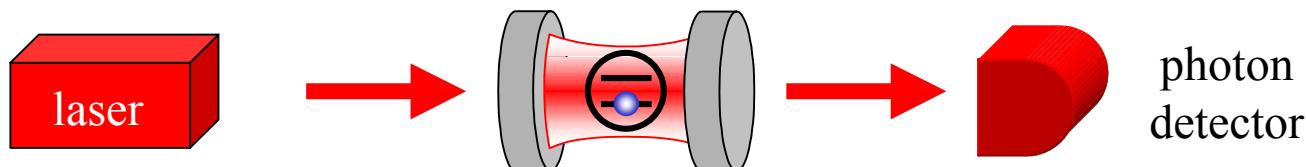
small  $\omega$ , large  $\mu$ , large  $V$



- + quantum manipulations at the single-atom and single-photon level
- photons at rest
- poor scalability and poor prospects for quantum communications

## optical domain (Caltech, MPQ, ...):

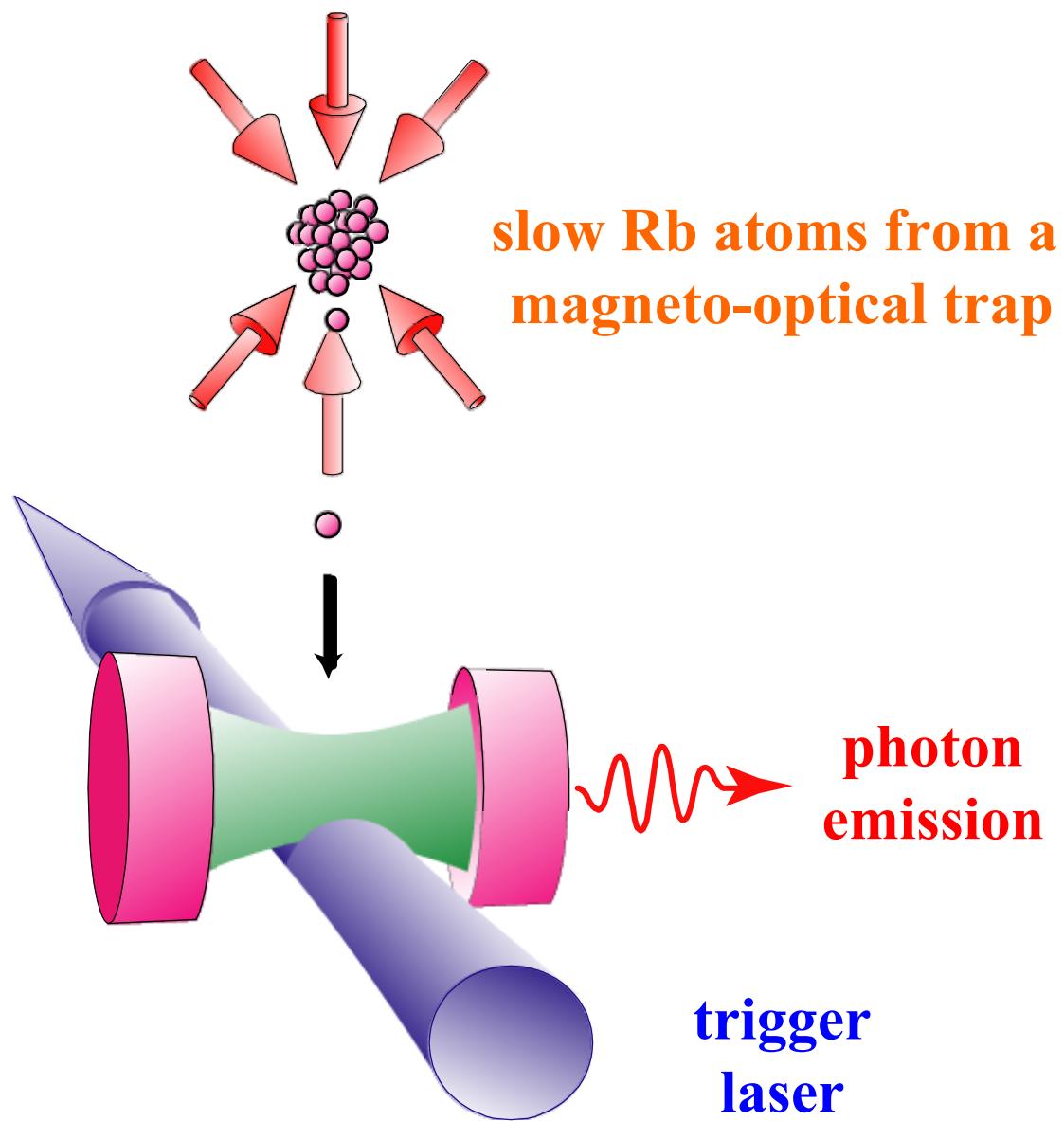
large  $\omega$ , small  $\mu$ , small  $V$



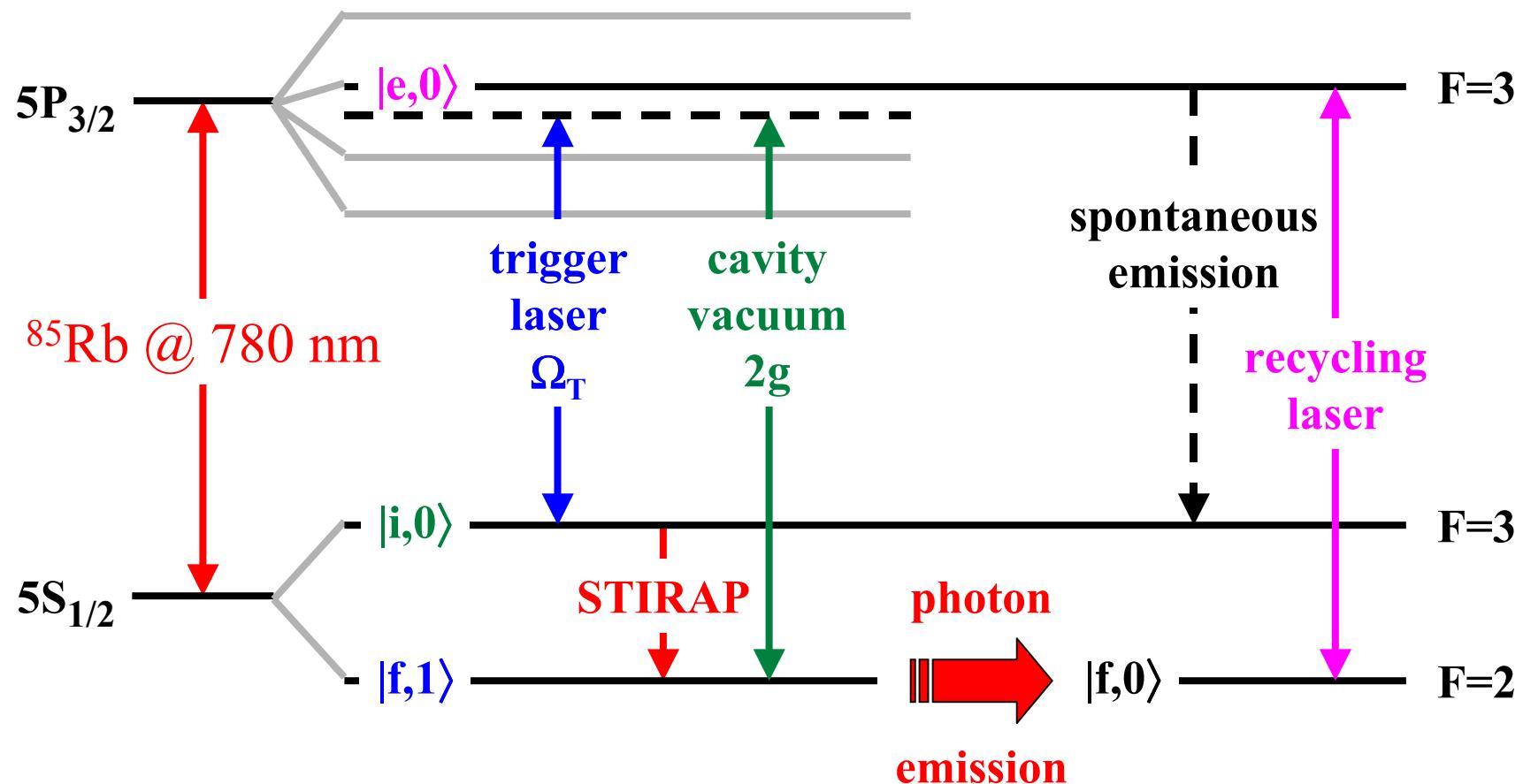
- + flying photons
- + good scalability and good prospects for quantum communications
- limited control over relevant parameters (atomic motion)

# Experimental Setup

**finesse = 60 000**  
**length = 1 mm**  
**waist = 35  $\mu$ m**



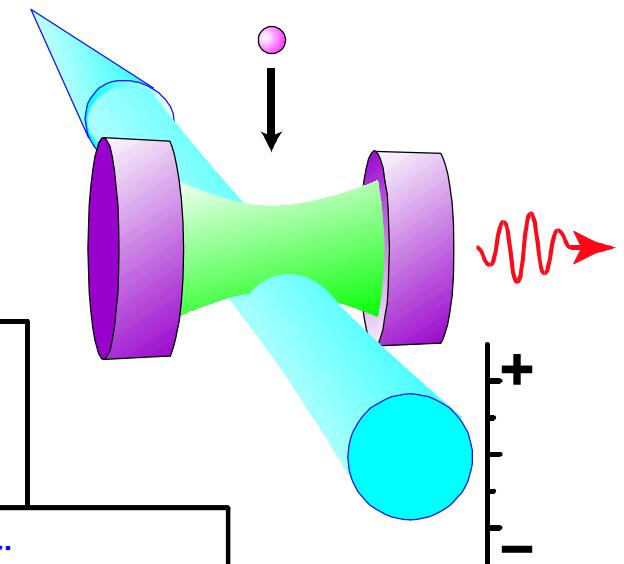
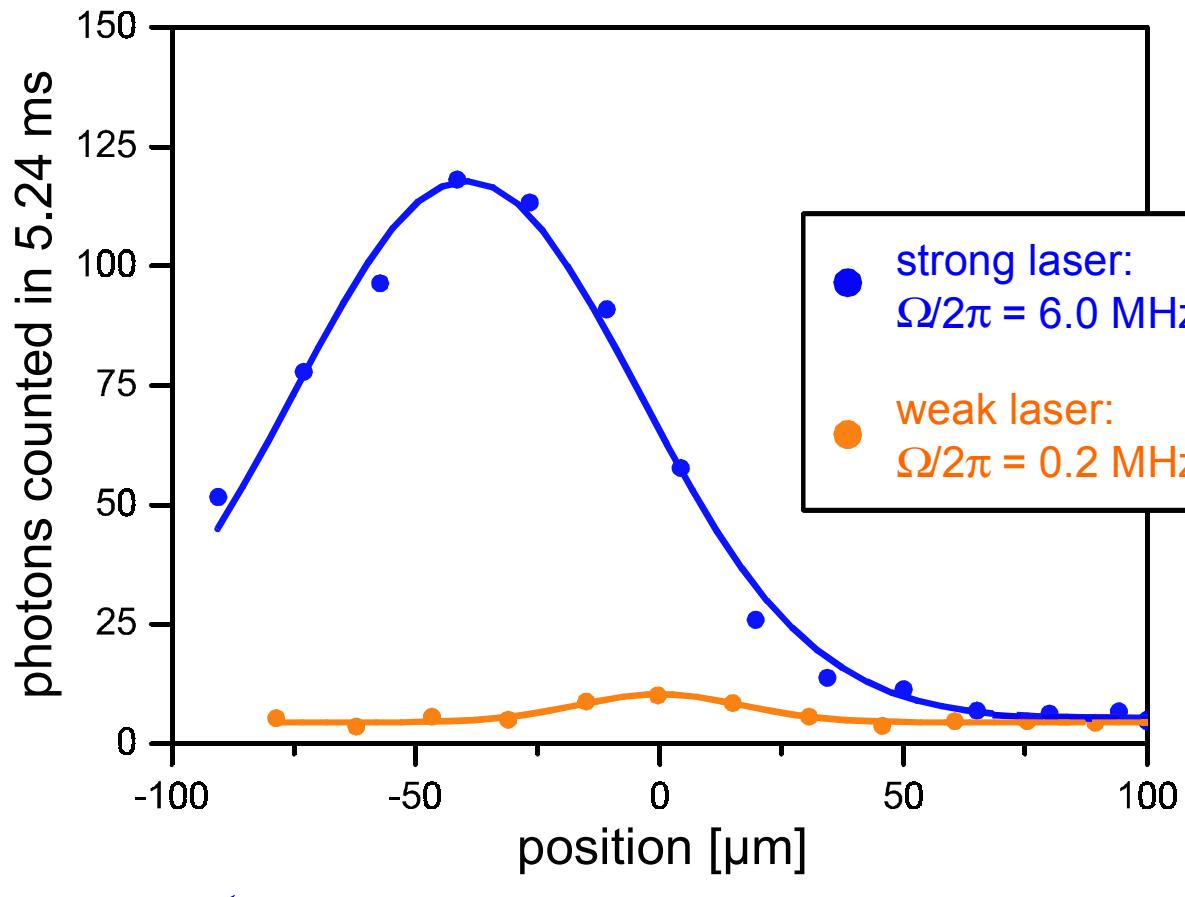
# Ingredient II: Stimulated Raman Adiabatic Passage



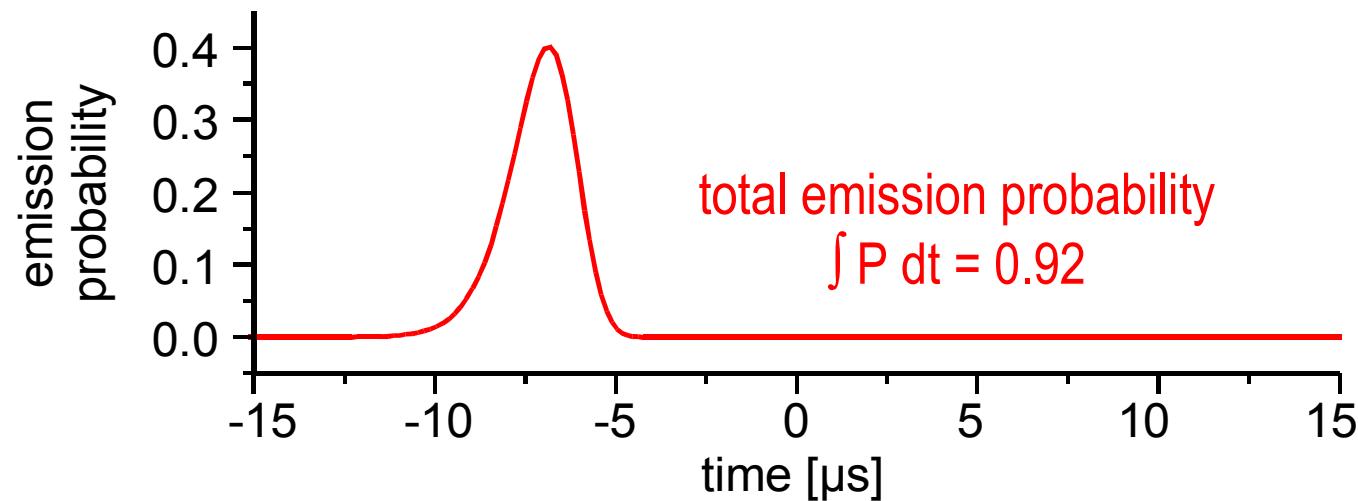
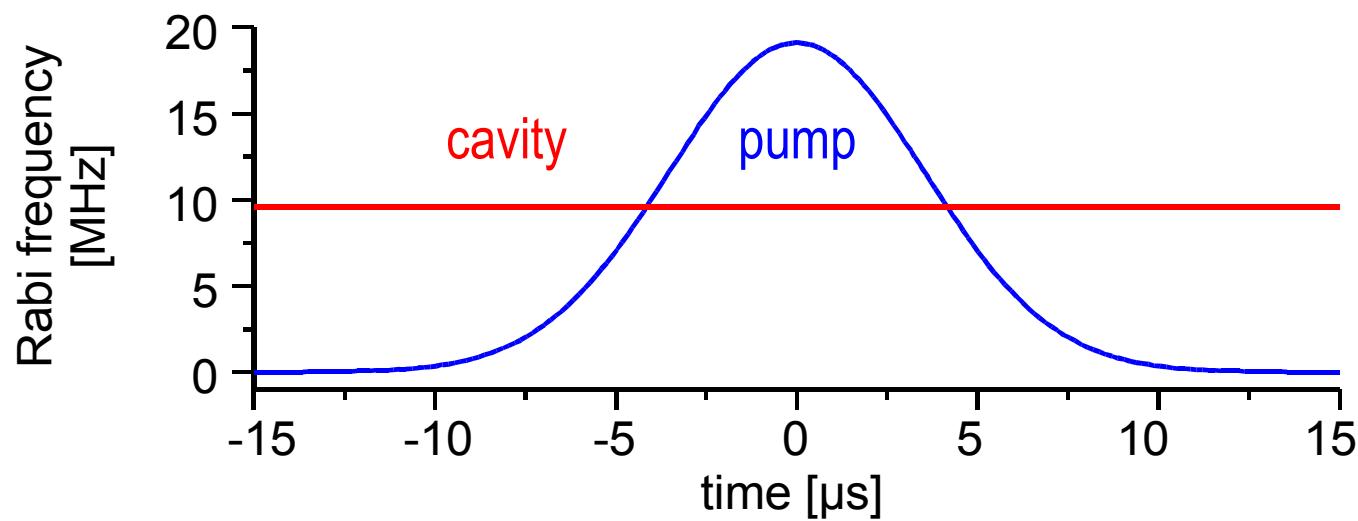
dark state (without contribution from the atom's excited state):

$$|\Psi_0(t)\rangle = \frac{2g(t)|i,0\rangle - \Omega_T(t)|f,1\rangle}{\sqrt{4g^2 + \Omega_T^2}}$$

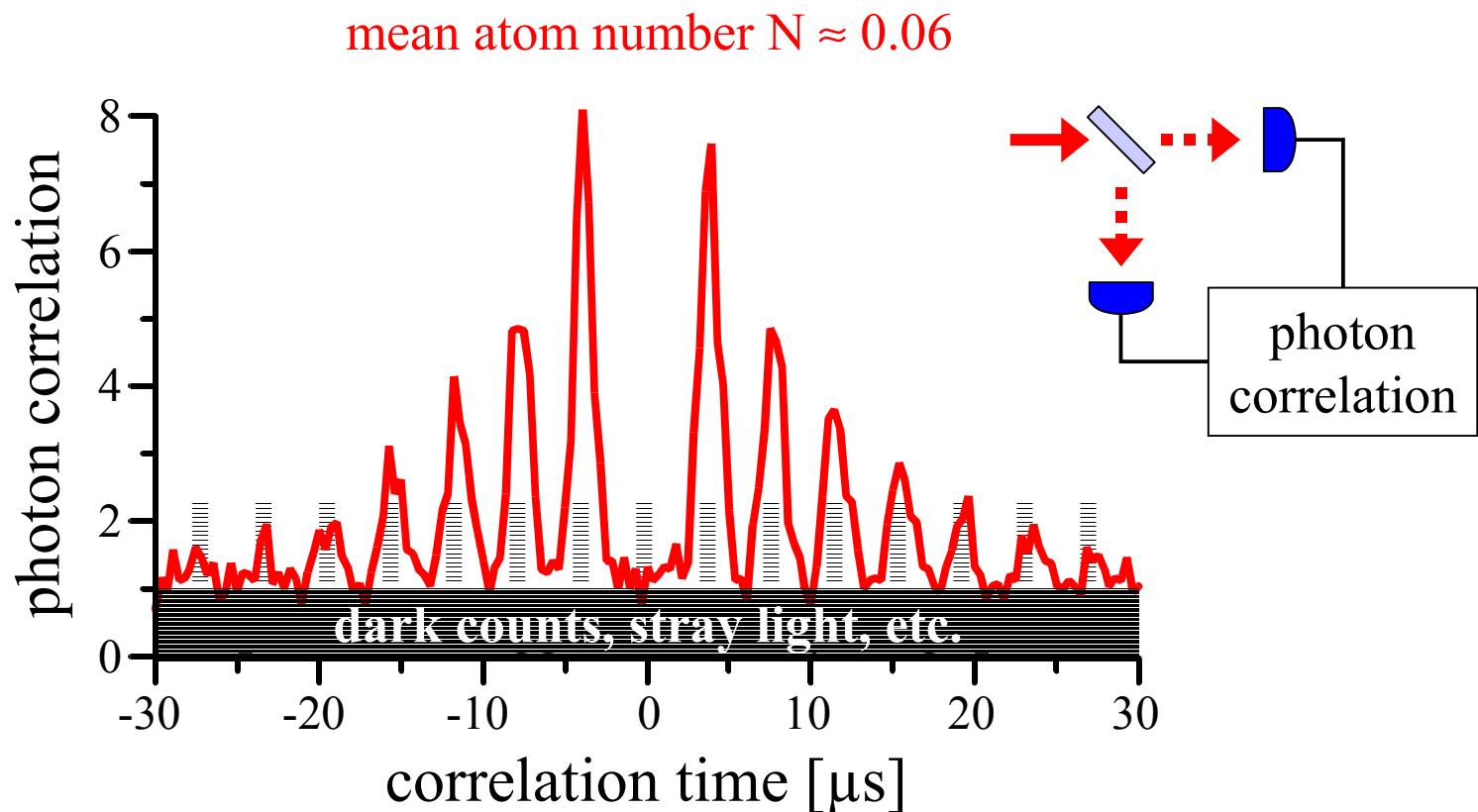
# Counterintuitive Interaction Sequence



# Numerical Simulation of a Single Shot



# Triggered Stream of Single-Photon Pulses

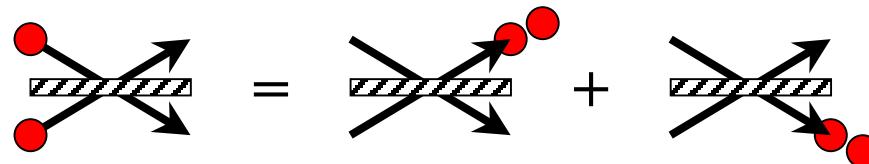


photon anti-bunching @  $\tau=0$   
successive photons @ successive pump pulses  
finite atom-cavity interaction time for a moving atom

# Single-Photon Physics – An Outlook

## Quantum computing:

- quantum gates with linear optics (Knill-LaFlamme-Milburn)
- interference of indistinguishable photons (Hong-Ou-Mandel)

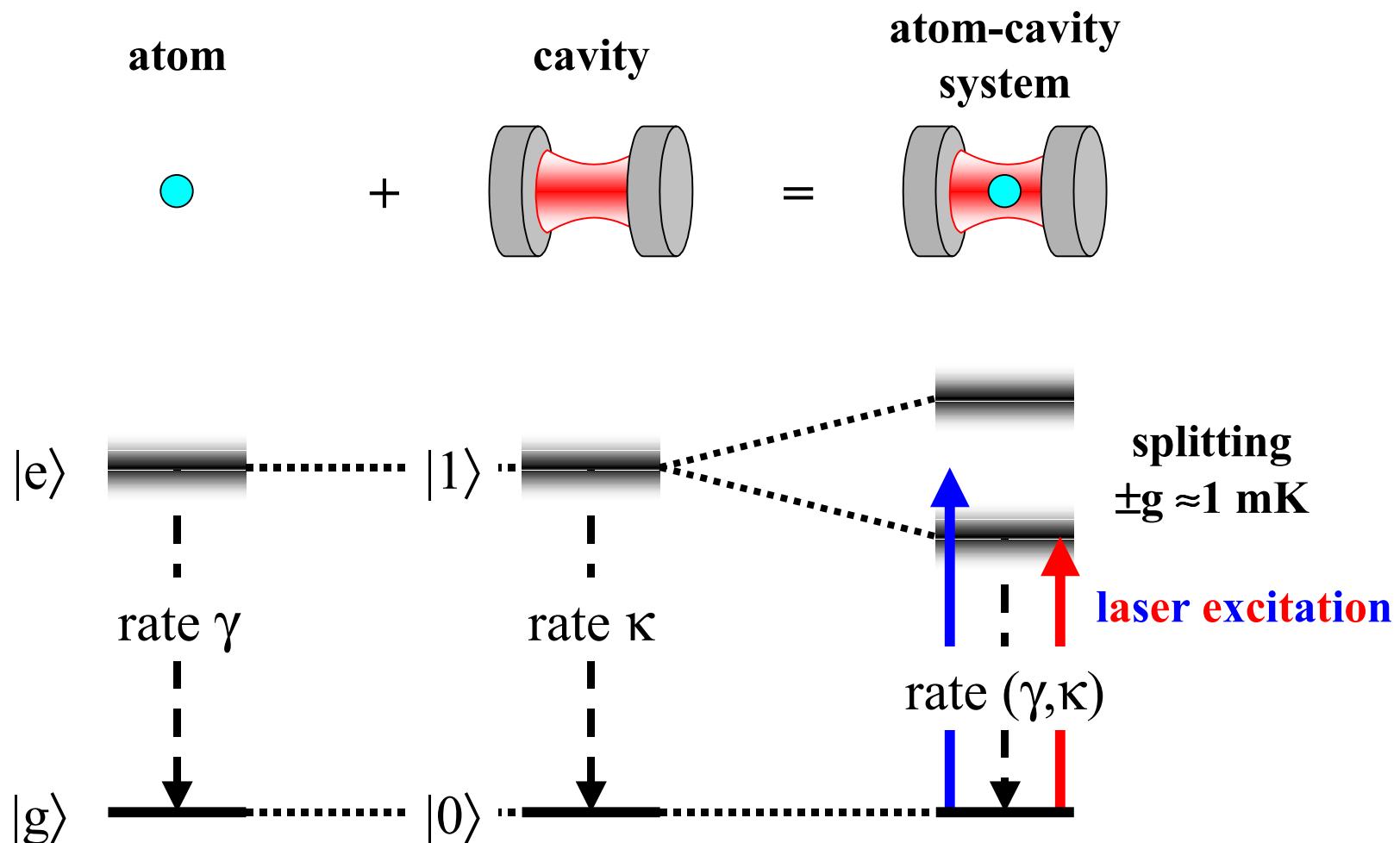


## Quantum networking:

- entanglement of two distant intra-cavity atoms
- teleportation of internal and/or external atomic states

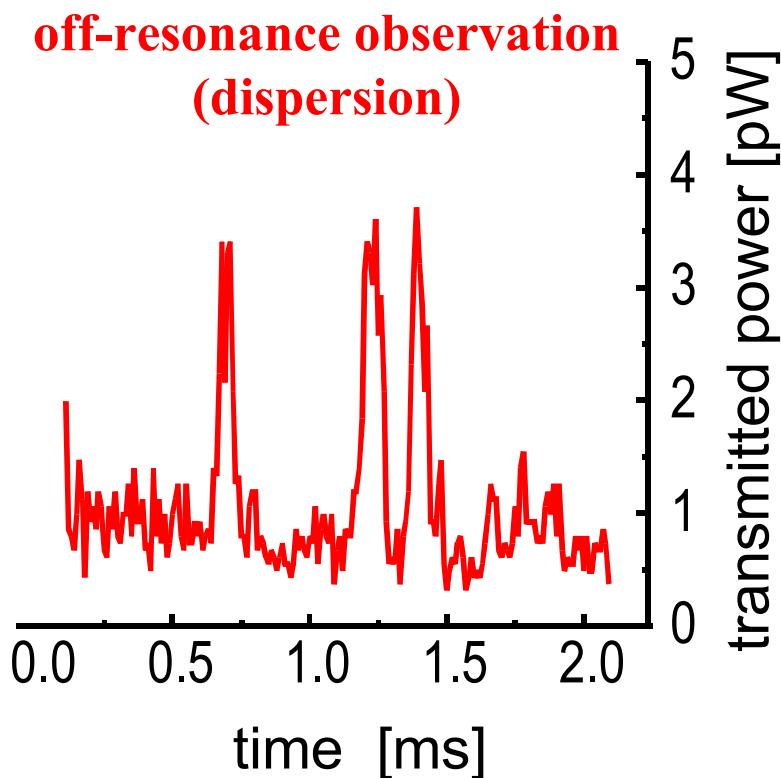
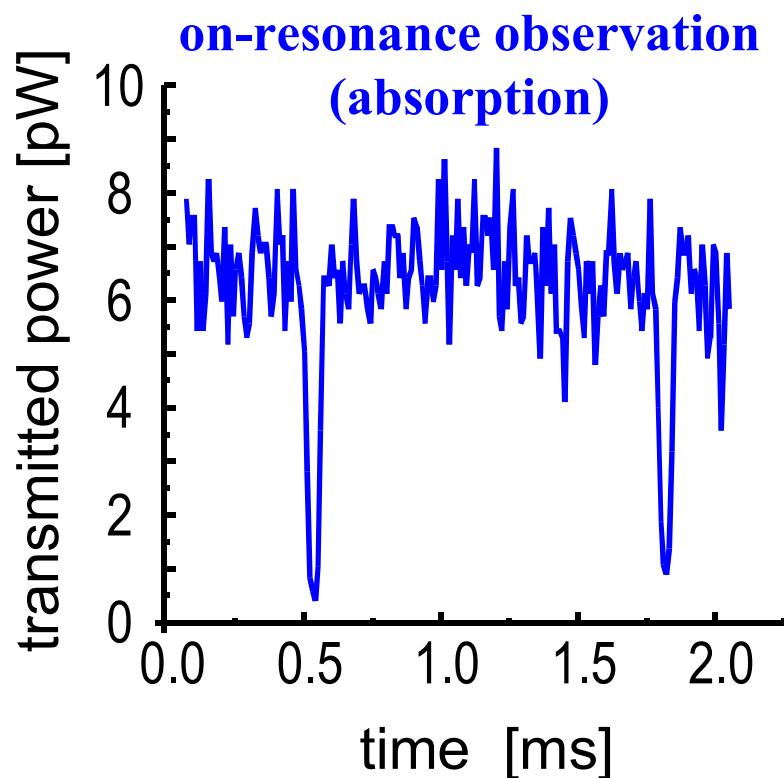
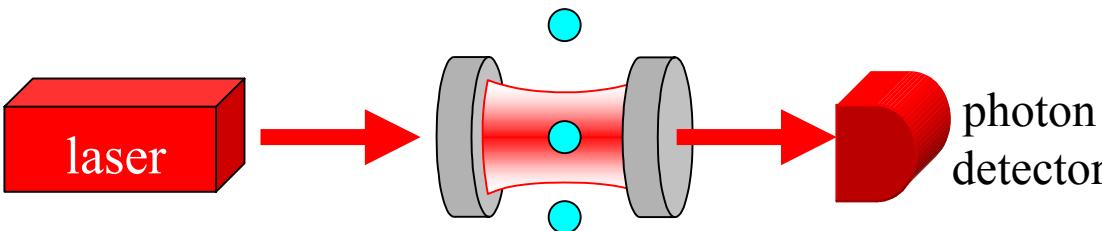


# Atom-Photon Molecule



Jaynes and Cummings, IEEE 51 (1963) 89

# Real-Time Observation of Individual Atoms



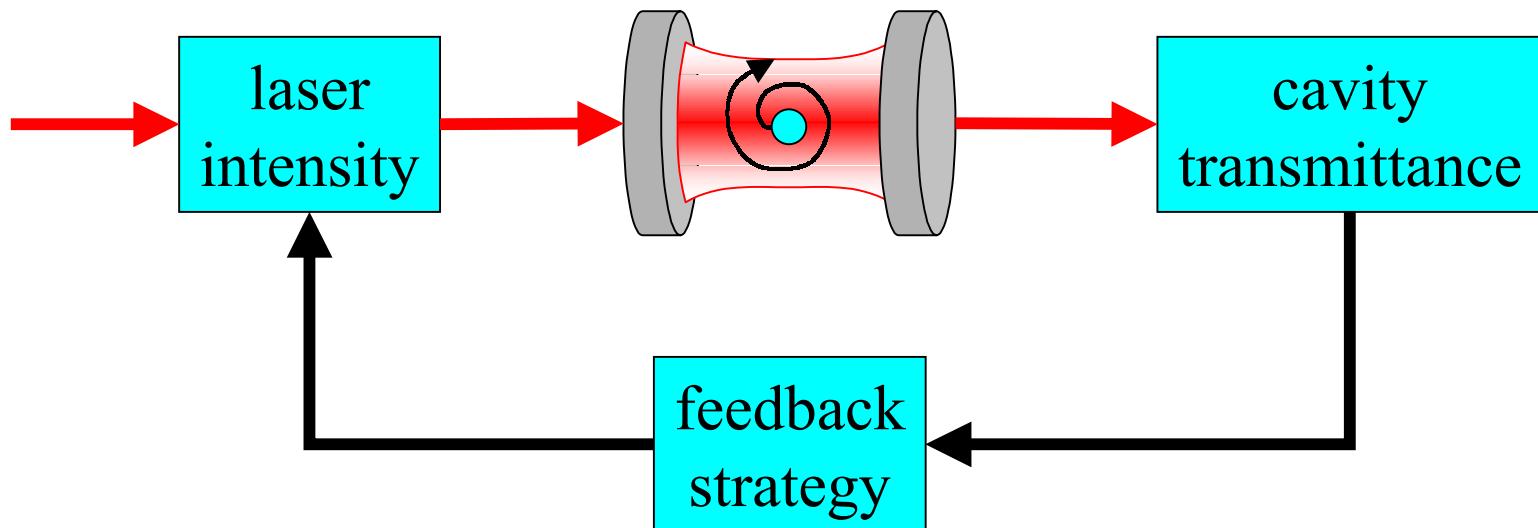
Mabuchi et al., Opt. Lett. **21** (1996) 1393

Münstermann et al., Opt. Commun. **159** (1999) 63

# Feedback Control of Atomic Motion

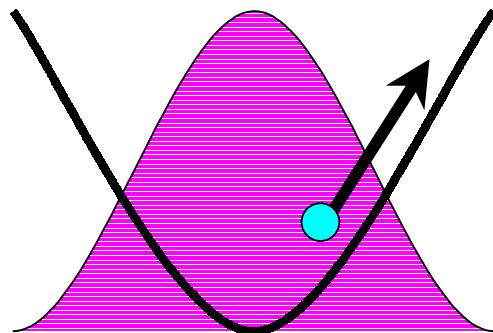
## real-time observation and mechanical binding:

- control an observed (dissipative) quantum system
- explore limits set by quantum noise and measurement-induced back-action



# Differentiating Feedback Control

**light intensity depends on the atomic velocity**



**velocity outwards**  
⇒ **'large' intensity**  
⇒ **'large' deceleration**



**velocity inwards**  
⇒ **small intensity**  
⇒ **small acceleration**

## advantage:

parametric cooling with phase automatically adjusted  
(but only one-dimensional cooling along radial direction)

# Average Exit Times

$150 \mu\text{s} +$   
 **$298(18) \mu\text{s}$**



$150 \mu\text{s} +$   
 **$395(23) \mu\text{s}$**



$150 \mu\text{s} +$   
 **$401(15) \mu\text{s}$**



predetermined  
feedback

proportional  
feedback

differentiating  
feedback

storage time limited by heating due to random  
momentum kicks from spontaneous emission events

# Single-Atom Physics – An Outlook

## continuously observed quantum system:

- quantum-limited position measurement of a free particle

$$\text{standard quantum limit} \quad \Delta x_{SQL} = \sqrt{\frac{\hbar\tau}{2m}}$$

## high-resolution single-particle microscopy:

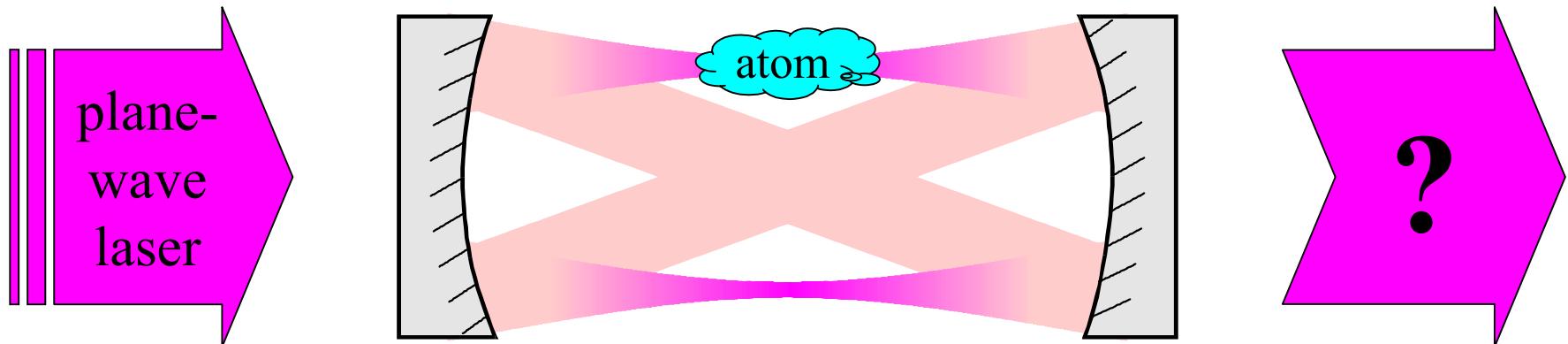
- real-time observation of atomic, biological or chemical processes

# **Real-time tracking of a single atom**

Hood et al.,  
Science **287** (2000) 1447

# Atomic-Position Measurement

in a resonator with **frequency-degenerate (transverse) modes**,  
the atom couples to a position-dependent subset of modes



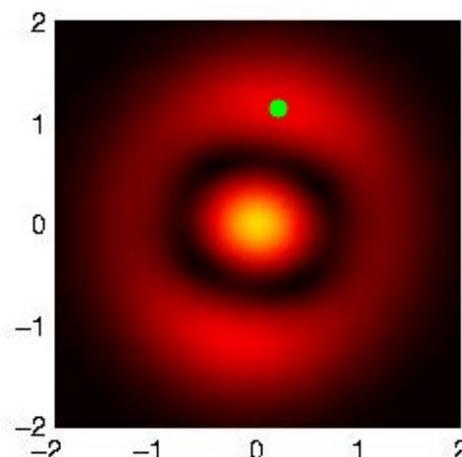
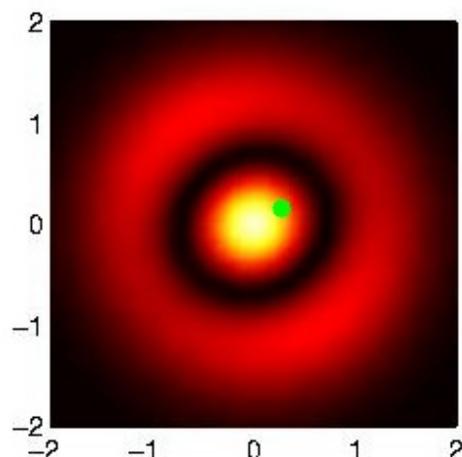
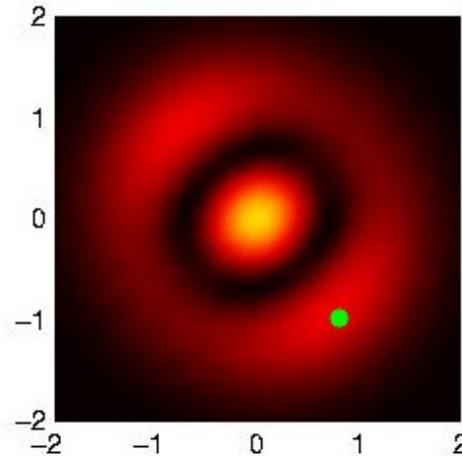
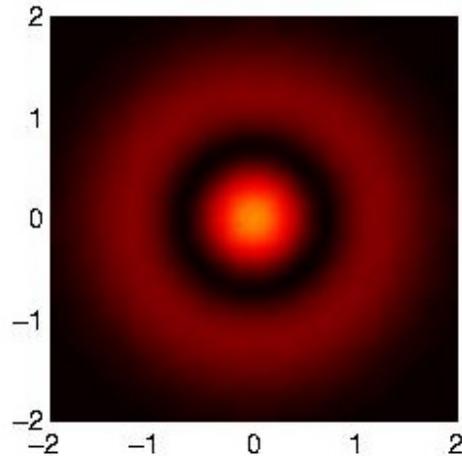
## additional advantages:

- \* small beam waist
- \* high position resolution
- \* strong coupling in a long cavity

see also Morin et al., Phys. Rev. Lett. 73 (1994) 1489

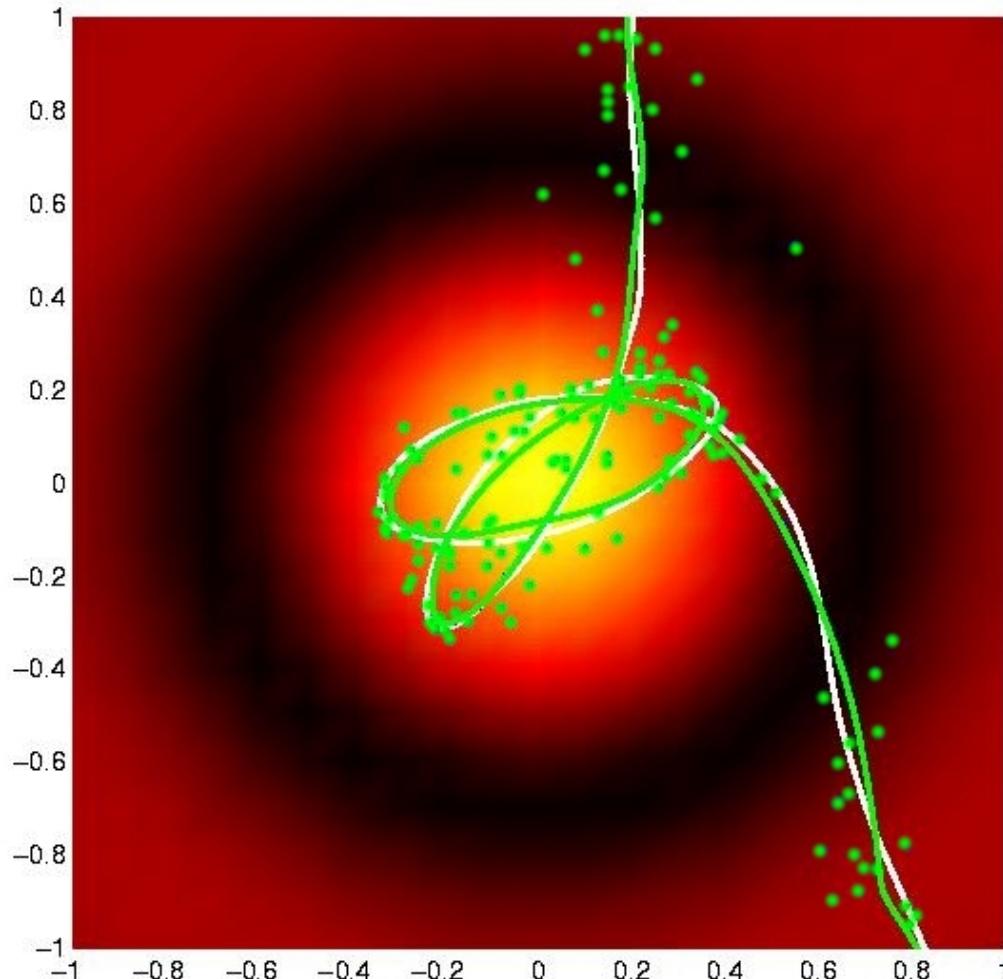
# Atomic Kaleidoscope (Simulation)

intensity pattern of the light transmitted through a cavity  
at the frequency of the transverse modes  $\text{TEM}_{2,0}$ ,  $\text{TEM}_{1,1}$  and  $\text{TEM}_{0,2}$



# Reconstruction of an Atomic Trajectory (Simulation)

based on the position-dependent differential phase shift  
of transverse modes  $\text{TEM}_{2,0}$ ,  $\text{TEM}_{1,1}$  and  $\text{TEM}_{0,2}$



Horak et al., Phys. Rev. Lett. **88** (2002) 043601

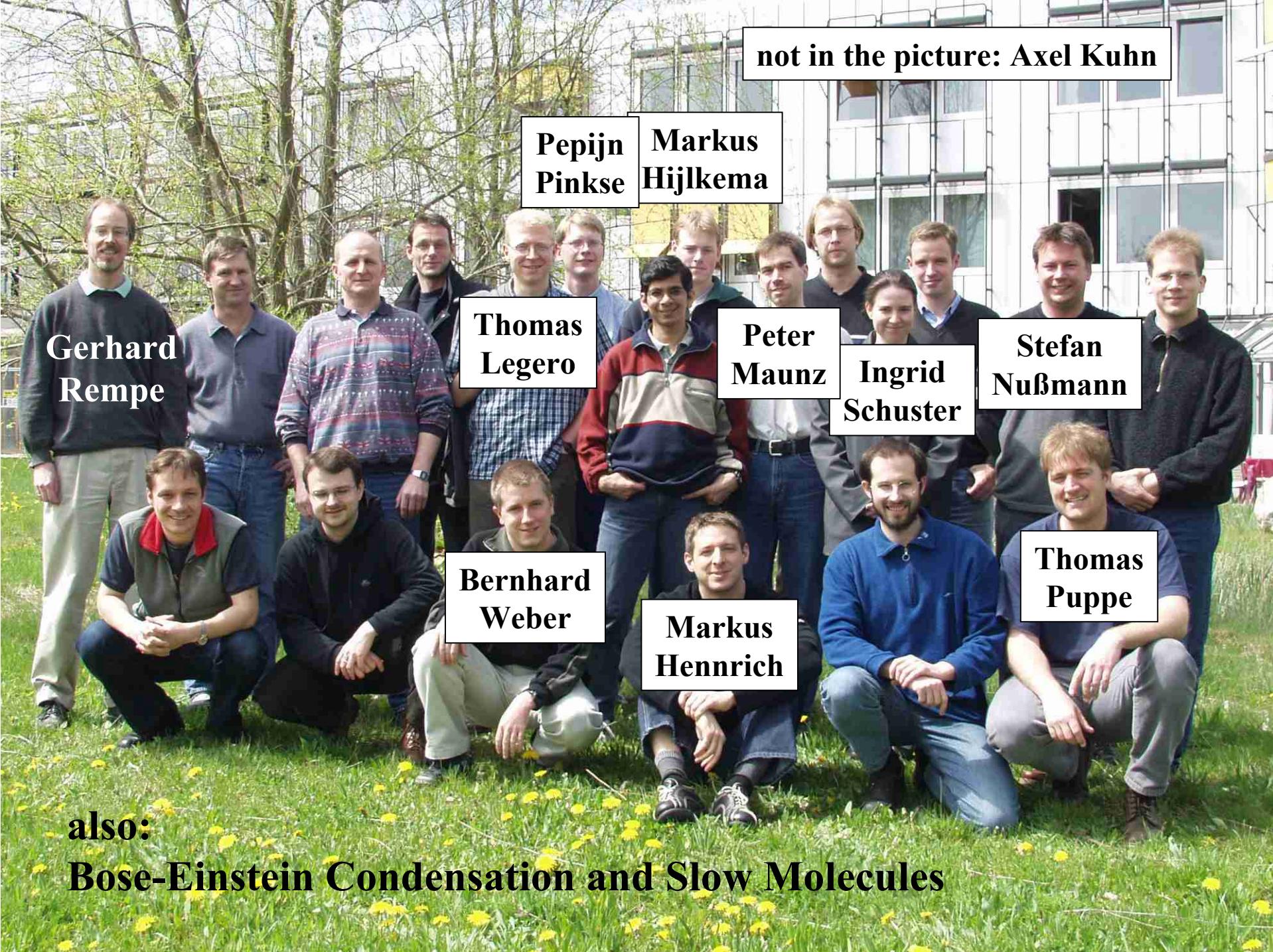
# Summary

cavity QED allows one to

- generate by means of
- a unitary process
- single photons
- on demand,

and

- observe
- and control
- with high spatial ( $\mu\text{m}$ )
- and temporal ( $\mu\text{s}$ ) resolution
- the motion of an individual atom.



not in the picture: Axel Kuhn

Pepijn  
Pinkse

Markus  
Hijkema

Thomas  
Legero

Peter  
Maunz

Stefan  
Nußmann

Gerhard  
Rempe

Ingrid  
Schuster

Bernhard  
Weber

Markus  
Hennrich

Thomas  
Puppe

also:

Bose-Einstein Condensation and Slow Molecules